

Consistent comparison in C++20

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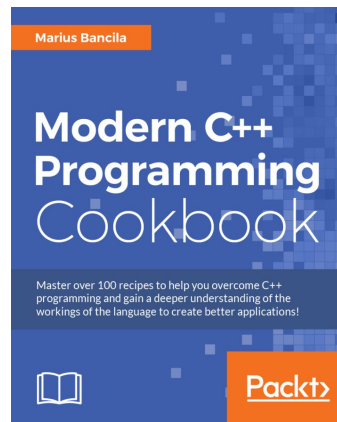
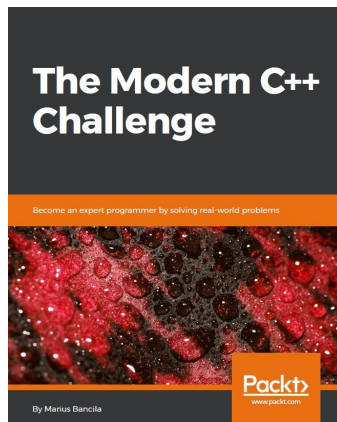
<https://github.com/mariusbancila>



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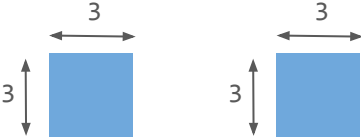
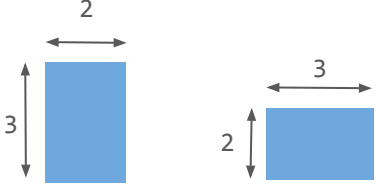
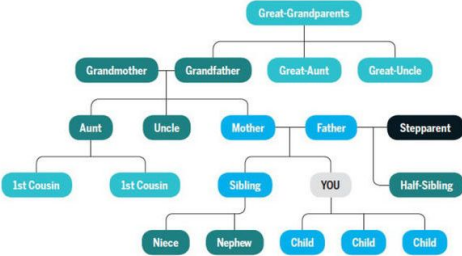


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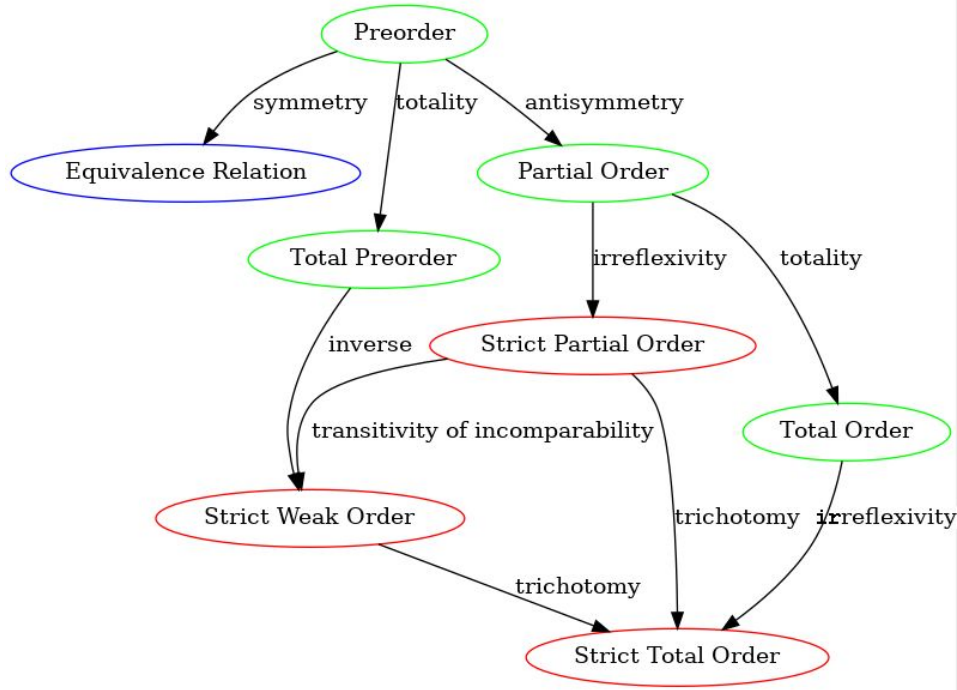


Agenda

- Ordering theory
- How to implement as of C++17
- Rules / best practices
- 3-way comparison operator in C++20
- Comparison categories
- Conversion
- Examples
- Rules / best practices
- And more...

Integers	..., -3, -2, -1, 0, 1, 2, 3, ...	equality, total ordering
Floating point	..., -1.5, 0, 3.14, 19.99, 42, ...	equality, partial ordering
Complex numbers	..., $1 + 2i$, $3 - i$, $-2 + 2i$, $3 + i$, ...	equality
IPs	192.168.0.1, 10.11.1.1, ...	equality, total ordering
Squares		equality, total ordering
Rectangles		equivalence
Family tree		equality, partial ordering

Order theory



- **Equivalence:** Binary relation that is
 - Reflexive
 $f(x,x) = \text{true}$
 - Symmetric
If $f(x, y)$ then $f(y, x)$
 - Transitive
If $f(x, y)$ and $f(y, z)$ then $f(x, z)$Where $f(x,y)$ is a comparison function
- **Equality:** Special equivalence relation where every element is equal to and only to itself
- **Preorder:** binary relation that is reflexive and transitive
- **Partial order:** binary relation that is reflexive, transitive, antisymmetric
- **Total order:** a binary relation that is reflexive, transitive, antisymmetric and total (i.e. no incomparable elements)

Jonathan Müller

<https://foonathan.net/blog/2018/07/19/ordering-relations-math.html>

How to implement comparison

Comparison functions (the C style)

	less	equal	greater
<code>memcmp</code>	<0	0	>0
<code>strcmp</code>	<0	0	>0
<code>strcoll</code>	<0	0	>0

Operators

- Operator `==` and `<`
- Operators `!=`, `>`, `<=`, `>=` can be implemented in terms of the other two

Functors

ipv4 class

```
struct ipv4
{
    explicit ipv4(unsigned char const a = 0,
                 unsigned char const b = 0,
                 unsigned char const c = 0,
                 unsigned char const d = 0) noexcept :
        data{a,b,c,d}
    {}

    unsigned long to_ulong() const noexcept
    {
        return
            (static_cast<unsigned long>(data[0]) << 24) |
            (static_cast<unsigned long>(data[1]) << 16) |
            (static_cast<unsigned long>(data[2]) << 8) |
            static_cast<unsigned long>(data[3]);
    }

private:
    std::array<unsigned char, 4> data;
};
```

```
ipv4 a1 { 192, 169, 0, 1 };
ipv4 a2 = a1;
ipv4 a3 = std::move(a2);
```

```
assert(a1 == a3);  assert(a1 > a4);
```

```
friend bool operator==(ipv4 const & a1, ipv4 const & a2) noexcept  
{ return a1.data == a2.data; }
```

```
friend bool operator!=(ipv4 const & a1, ipv4 const & a2) noexcept  
{ return !(a1 == a2); }
```

```
friend bool operator<(ipv4 const & a1, ipv4 const & a2) noexcept  
{ return a1.to_ulong() < a2.to_ulong(); }
```

```
friend bool operator>(ipv4 const & a1, ipv4 const & a2) noexcept  
{ return a2 < a1; }
```

```
friend bool operator<=(ipv4 const & a1, ipv4 const & a2) noexcept  
{ return !(a2 < a1); }
```

```
friend bool operator>=(ipv4 const & a1, ipv4 const & a2) noexcept  
{ return !(a1 < a2); }
```



```
assert(a1 == 0xC0A90001);
```

```
friend bool operator==(ipv4 const & a1, unsigned long const a2) noexcept  
{ return a1.to_ulong() == a2; }
```

```
friend bool operator!=(ipv4 const & a1, unsigned long const a2) noexcept  
{ return a1 != a2; }
```

```
friend bool operator<(ipv4 const & a1, unsigned long const a2) noexcept  
{ return a1.to_ulong() < a2; }
```

```
friend bool operator>(ipv4 const & a1, unsigned long const a2) noexcept  
{ return a1.to_ulong() > a2; }
```

```
friend bool operator<=(ipv4 const & a1, unsigned long const a2) noexcept  
{ return a1.to_ulong() <= a2; }
```

```
friend bool operator>=(ipv4 const & a1, unsigned long const a2) noexcept  
{ return !(a1 < a2); }
```

```
assert(0xC0A90001 == a1);
```

```
friend bool operator==(unsigned long const a1, ipv4 const & a2) noexcept  
{ return a1 == a2.to_ulong(); }
```

```
friend bool operator!=(unsigned long const a1, ipv4 const & a2) noexcept  
{ return a1 != a2; }
```

```
friend bool operator<(unsigned long const a1, ipv4 const & a2) noexcept  
{ return a1 < a2.to_ulong(); }
```

```
friend bool operator>(unsigned long const a1, ipv4 const & a2) noexcept  
{ return a1 > a2.to_ulong(); }
```

```
friend bool operator<=(unsigned long const a1, ipv4 const & a2) noexcept  
{ return a1 <= a2.to_ulong(); }
```

```
friend bool operator>=(unsigned long const a1, ipv4 const & a2) noexcept  
{ return !(a1 < a2); }
```

and more...

```
ipv4 from_string(std::string_view text)
{
    unsigned char a = 0, b = 0, c = 0, d = 0;
    int result = sscanf(text.data(), "%hhu.%hhu.%hhu.%hhu", &a, &b, &c, &d);
    if (result != 4) throw std::runtime_error("invalid IPv4 address");
    return ipv4{ a,b,c,d };
}
```

```
ipv4 a5 = from_string("192.169.0.1");
assert(a1 == a5);
```

```
assert(a1 == "192.169.0.1");
```

```
inline bool operator==(ipv4 const & a1, char const * const a2)  
{ return a1 == from_string(a2); }
```

```
inline bool operator!=(ipv4 const & a1, char const * const a2)  
{ return a1 != a2; }
```

```
inline bool operator<(ipv4 const & a1, char const * const a2)  
{ return a1 < from_string(a2); }
```

```
inline bool operator>(ipv4 const & a1, char const * const a2)  
{ return a1 > from_string(a2); }
```

```
inline bool operator<=(ipv4 const & a1, char const * const a2)  
{ return a1 <= from_string(a2); }
```

```
inline bool operator>=(ipv4 const & a1, char const * const a2)  
{ return !(a1 < a2); }
```

```
assert("192.169.0.1" == a1);
```

```
inline bool operator==(char const * const a1, ipv4 const & a2)  
{ return from_string(a1) == a2; }
```

```
inline bool operator!=(char const * const a1, ipv4 const & a2)  
{ return a1 != a2; }
```

```
inline bool operator<(char const * const a1, ipv4 const & a2)  
{ return from_string(a1) < a2; }
```

```
inline bool operator>(char const * const a1, ipv4 const & a2)  
{ return from_string(a1) > a2; }
```

```
inline bool operator<=(char const * const a1, ipv4 const & a2)  
{ return from_string(a1) <= a2; }
```

```
inline bool operator>=(char const * const a1, ipv4 const & a2)  
{ return !(a1 < a2); }
```

```

struct ipv4
{
    explicit ipv4(unsigned char const a = 0,
                 unsigned char const b = 0,
                 unsigned char const c = 0,
                 unsigned char const d = 0) noexcept;
    unsigned long to_ulong() const noexcept;

    friend bool operator==(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator!=(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator<(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator>(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator<=(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator>=(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator==(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator!=(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator<(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator>(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator<=(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator>=(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator==(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator!=(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator<(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator>(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator<=(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator>=(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator==(ipv4 const & a1, char const * const a2);
    friend bool operator!=(ipv4 const & a1, char const * const a2);
    friend bool operator<(ipv4 const & a1, char const * const a2);
    friend bool operator>(ipv4 const & a1, char const * const a2);
    friend bool operator<=(ipv4 const & a1, char const * const a2);
    friend bool operator>=(ipv4 const & a1, char const * const a2);
    friend bool operator==(char const * const a1, ipv4 const & a2);
    friend bool operator!=(char const * const a1, ipv4 const & a2);
    friend bool operator<(char const * const a1, ipv4 const & a2);
    friend bool operator>(char const * const a1, ipv4 const & a2);
    friend bool operator<=(char const * const a1, ipv4 const & a2);
    friend bool operator>=(char const * const a1, ipv4 const & a2);
private:
    std::array<unsigned char, 4> data;
};

```

Overload the equality and comparison operators as non-member functions...

If you want the first operand to be of a type that is not this class, or
If you want implicit type conversion for any of the two operands

Implement an equality relation only if you know the value of the type.

Implement equality by comparing the properties that form the value.

Copies must be equal.

Implement deep equality when you have
deep copy.

Implement shallow equality when you
have shallow copy.

In you overload any of $<$, $<=$, $>$, $>=$
implement all of them.

In you overload the comparison operators also overload the equality operators.

The comparison operators should implement a total ordering.

For any other ordering implement a named predicate.

The comparison operators should implement an ordering inducing equality, not just equivalence.

```

struct ipv4
{
    explicit ipv4(unsigned char const a = 0,
                 unsigned char const b = 0,
                 unsigned char const c = 0,
                 unsigned char const d = 0) noexcept;
    unsigned long to_ulong() const noexcept;

    friend bool operator==(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator!=(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator<(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator>(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator<=(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator>=(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator==(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator!=(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator<(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator>(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator<=(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator>=(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator==(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator!=(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator<(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator>(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator<=(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator>=(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator==(ipv4 const & a1, char const * const a2);
    friend bool operator!=(ipv4 const & a1, char const * const a2);
    friend bool operator<(ipv4 const & a1, char const * const a2);
    friend bool operator>(ipv4 const & a1, char const * const a2);
    friend bool operator<=(ipv4 const & a1, char const * const a2);
    friend bool operator>=(ipv4 const & a1, char const * const a2);
    friend bool operator==(char const * const a1, ipv4 const & a2);
    friend bool operator!=(char const * const a1, ipv4 const & a2);
    friend bool operator<(char const * const a1, ipv4 const & a2);
    friend bool operator>(char const * const a1, ipv4 const & a2);
    friend bool operator<=(char const * const a1, ipv4 const & a2);
    friend bool operator>=(char const * const a1, ipv4 const & a2);
private:
    std::array<unsigned char, 4> data;
};

```


std::rel_ops

```
namespace rel_ops
{
    template <class T>
    bool operator!=( const T& lhs, const T& rhs )
    { return !(lhs == rhs); }

    template <class T>
    bool operator>( const T& lhs, const T& rhs )
    { return rhs < lhs; }

    template <class T>
    bool operator<=( const T& lhs, const T& rhs )
    { return !(rhs < lhs); }

    template <class T>
    bool operator>=( const T& lhs, const T& rhs )
    { return !(lhs < rhs); }
}
```

```
struct ipv4
{ /* ... */ };

friend bool
operator==(ipv4 const & a1, ipv4 const & a2) noexcept
{ return a1.data == a2.data; }

friend bool
operator<(ipv4 const & a1, ipv4 const & a2) noexcept
{ return a1.to_ulong() < a2.to_ulong(); }

int main()
{
    ipv4 a1 { 192, 169, 0, 1 };
    ipv4 a2 { 168, 52, 77, 101 };

    using namespace std::rel_ops;
    assert(a1 != a2);
    assert(a1 > a2);
}
```

std::rel_ops

```
namespace rel_ops
{
    template <class T>
    bool operator!=( const T& lhs, const T& rhs )
    { return !(lhs == rhs); }

    template <class T>
    bool operator>( const T& lhs, const T& rhs )
    { return rhs < lhs; }

    template <class T>
    bool operator<( const T& lhs, const T& rhs )
    { return !(rhs < lhs); }

    template <class T>
    bool operator>=( const T& lhs, const T& rhs )
    { return !(lhs < rhs); }
}
```

```
struct ipv4
{ /* ... */ };

friend bool
operator==( const ipv4& a1, const ipv4& a2 ) noexcept
{ return a1.data == a2.data; }

friend bool
operator<( ipv4 const & a1, ipv4 const & a2 ) noexcept
{ return a1.to_ulong() < a2.to_ulong(); }

int main()
{
    ipv4 a1 { 192, 169, 0, 1 };
    ipv4 a2 { 168, 52, 77, 101 };

    using namespace std::rel_ops;
    assert(a1 != a2);
    assert(a1 > a2);
}
```

spaceship operator $\langle = \rangle$



<https://scifi.stackexchange.com>

TIE fighter operator |=|



http://disney.wikia.com/wiki/TIE_Fighter

three-way comparison operator

Three-way comparison operator...

- Is overloadable
- Has precedence higher than `<` and lower than `<<`
- Returns a type comparable against 0
 - Other return types are allowed
- In the standard return a standard comparison category type
- Is for type implementers only
- Supported (partially) in Clang 7, VC++ 2019

ipv4 rewritten in C++20

```
struct ipv4
{
    explicit ipv4(unsigned char const a = 0,
                 unsigned char const b = 0,
                 unsigned char const c = 0,
                 unsigned char const d = 0) noexcept;
    unsigned long to_ulong() const noexcept;

    auto operator<=>(ipv4 const & rhv) const noexcept = default;

    std::strong_ordering operator<=>(unsigned long const a) const noexcept
    {
        return to_ulong() <=> a;
    }

    std::strong_ordering operator<=>(char const * const a) const
    {
        return *this <=> from_string(a);
    }

private:
    std::array<unsigned char, 4> data;
};
```

ipv4 rewritten in C++20

```
struct ipv4
{
    explicit ipv4(unsigned char const a = 0,
                 unsigned char const b = 0,
                 unsigned char const c = 0,
                 unsigned char const d = 0) noexcept;
    unsigned long to_ulong() const noexcept;

    auto operator<=>(ipv4 const & rhv) const noexcept = default;

    std::strong_ordering operator<=>(unsigned long const a) const noexcept
    {
        return to_ulong() <=> a;
    }

    std::strong_ordering operator<=>(char const * const a) const
    {
        return *this <=> from_string(a);
    }

private:
    std::array<unsigned char, 4> data;
};
```

```
struct ipv4
{
    explicit ipv4(unsigned char const a = 0,
                 unsigned char const b = 0,
                 unsigned char const c = 0,
                 unsigned char const d = 0) noexcept;
    unsigned long to_ulong() const noexcept;

    friend bool operator==(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator!=(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator<(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator>(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator<=(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator>=(ipv4 const & a1, ipv4 const & a2) noexcept;
    friend bool operator==(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator!=(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator<(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator>(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator<=(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator>=(ipv4 const & a1, unsigned long const a2) noexcept;
    friend bool operator==(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator!=(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator<(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator>(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator<=(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator>=(unsigned long const a1, ipv4 const & a2) noexcept;
    friend bool operator==(ipv4 const & a1, char const * const a2);
    friend bool operator!=(ipv4 const & a1, char const * const a2);
    friend bool operator<(ipv4 const & a1, char const * const a2);
    friend bool operator>(ipv4 const & a1, char const * const a2);
    friend bool operator<=(ipv4 const & a1, char const * const a2);
    friend bool operator>=(ipv4 const & a1, char const * const a2);
    friend bool operator==(char const * const a1, ipv4 const & a2);
    friend bool operator!=(char const * const a1, ipv4 const & a2);
    friend bool operator<(char const * const a1, ipv4 const & a2);
    friend bool operator>(char const * const a1, ipv4 const & a2);
    friend bool operator<=(char const * const a1, ipv4 const & a2);
    friend bool operator>=(char const * const a1, ipv4 const & a2);

private:
    std::array<unsigned char, 4> data;
};
```


Overload the three-way comparison operator as member functions.

Even if you want the first operand to be of a type that is not this class

Overload the three-way comparison operator as non-member functions.

Only if you want implicit conversion on both arguments
(compare two objects neither of which is of this type)

```
struct foo
{
    foo(int const x)
        : data{ x } {}
    foo(std::string_view x)
        : data{ std::stoi(x.data()) } {}

private:
    int data;

    friend auto operator<=>(foo const & lhs, foo const & rhs) noexcept;
};

inline auto operator<=>(foo const & lhs, foo const & rhs) noexcept
{
    return lhs.data <=> rhs.data;
}

assert(foo{ 42 } == foo{ "42" });
assert(42 == std::string_view{ "42" });
```

```

struct foo
{
    foo(int const x)
        : data{ x } {}
    foo(std::string_view x)
        : data{ std::stoi(x.data()) } {}

private:
    int data;

    friend auto operator<=>(foo const & lhs, foo const & rhs) noexcept;
};

inline auto operator<=>(foo const & lhs, foo const & rhs) noexcept
{
    return lhs.data <=> rhs.data;
}

assert(foo{ 42 } == foo{ "42" });
assert(42 == std::string_view{ "42" });

```

```

struct A
{
    int i;
};

struct B
{
    B(A a) : i(a.i) {}

    int i;
};

inline auto
operator<=>(B const& lhs, B const& rhs) const noexcept
{
    return lhs.i <=> rhs.i;
}

assert(A{ 2 } == A{ 2 });
assert(A{ 2 } < A{ 1 });

```

Implement only the three-way operator.
Use only the two-way operators.

Memberwise comparison

Automatically implemented with strongest comparison

```
struct foo {  
    auto operator<=>(int const&) const noexcept = default;  
};
```

Automatically implemented with user-specified comparison

```
struct foo {  
    std::strong_ordering operator<=>(int const&) const noexcept = default;  
};
```

Non-memberwise comparison

```
class Project : public CostUnit
{
    int      id;
    int      type;
    std::string name;

public:
    std::strong_ordering operator<=>(const Project& other) const noexcept
    {
        if (auto cmp = (CostUnit&)(*this) <=> (CostUnit&)other; cmp != 0) return cmp;
        if (auto cmp = name <=> other.name; cmp != 0) return cmp;
        if (auto cmp = type <=> other.type; cmp != 0) return cmp;
        return id <=> other.id;
    }
};
```

```
Project p1, p2;
if(p1 == p2) { }
```

```
if(p1 < p2) { }
```

```
std::set<Project> s;
s.insert(p1);
```

Comparison categories

Category	Operators	Substitutability	Comparable values
<code>strong_ordering</code>	<code>==</code> , <code>!=</code> , <code><</code> , <code><=</code> , <code>></code> , <code>>=</code>	Yes	Yes
<code>weak_ordering</code>	<code>==</code> , <code>!=</code> , <code><</code> , <code><=</code> , <code>></code> , <code>>=</code>	No	Yes
<code>partial_ordering</code>	<code>==</code> , <code>!=</code> , <code><</code> , <code><=</code> , <code>></code> , <code>>=</code>	No	No
<code>strong_equality</code>	<code>==</code> , <code>!=</code>	Yes	
<code>weak_equality</code>	<code>==</code> , <code>!=</code>	No	

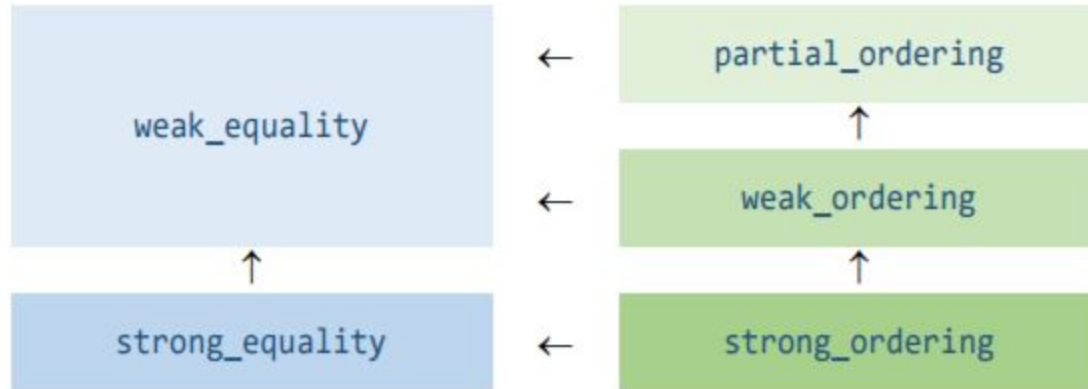
Substitutability

- If $a==b$, then $f(a)==f(b)$, where f is a function that reads only comparison-salient state accessible via the argument's public const members

Comparable values

- Yes: at least one of $a < b$, $a == b$, or $a > b$ must be true
- No: $a < b$, $a == b$, and $a > b$ may be all false

Conversions



Herb Sutter, P0515R2

Valid values

Category	Numeric values			Non-numeric values
	-1	0	+1	
strong_ordering	less	equal	greater	
		equivalent		
weak_ordering	less	equivalent	greater	
partial_ordering	less	equivalent	greater	unordered
strong_equality		equal	nonequal	
		equivalent	nonequivalent	
weak_equality		equivalent	nonequivalent	

operator<=> should return

Substitutability? $a==b \Rightarrow f(a)==f(b)$	Comparable values? $a<b, a==b, \text{ or } a>b$	Support $a < b$?	
		Yes	No
Yes	Yes	<code>std::strong_ordering</code>	<code>std::strong_equality</code>
No	Yes	<code>std::weak_ordering</code>	<code>std::weak_equality</code>
	No	<code>std::partial_ordering</code>	

Partial ordering example

```
struct Employee
{
    bool is_managed_by(Employee const&) const;
    bool is_manager_of(Employee const&) const;
    bool is_same(Employee const&) const;

    std::partial_ordering operator<=>(Employee const& other) const noexcept
    {
        if(is_same(other))
            return std::partial_ordering::equivalent;
        if(is_managed_by(other))
            return std::partial_ordering::less;
        if(is_manager_of(other))
            return std::partial_ordering::greater;
        return partial_ordering::unordered;
    }
};
```

The comparison operators should implement a total ordering.

For any other ordering implement a named predicate.

Implement operator `<=>` if your type should have *full ordering* (return `std::strong_ordering`) or *equality* (return `std::strong_equality`).

Otherwise, implement comparison as a named function.

Utilities

`std::compare_3way()`

- Compares values using operator `<=>` and produces the strongest applicable comparison category
- Falls back to two-way comparison operators

`std::lexicographical_compare_3way()`

- Lexicographic comparison of two ranges using operator `<=>`

`std::common_comparison_category`

- Alias for the strongest comparison category to which all of the template arguments can be converted to

std::pair's <=> possible implementation

```
template<class T1, class T2>
struct pair
{
    T1 first;
    T2 second;

    auto operator<=> (pair const& other) const
        -> std::common_comparison_category_t<
            decltype(std::compare_3way(first, other.first)),
            decltype(std::compare_3way(second, other.second))>
    {
        if (auto cmp = std::compare_3way(first, other.first); cmp != 0) return cmp;
        return std::compare3_way(second, other.second);
    }
}
```


Lexicographical comparison for ranges

```
std::vector<int> v {1, 1, 2, 3, 5, 8, 13};  
std::array<int, 7> a {1, 1, 2, 3, 5, 8, 13};
```

```
if(0 == std::lexicographical_compare_3way(  
    std::cbegin(v), std::cend(v),  
    std::cbegin(a), std::cend(a)))  
{  
    // are equal  
}
```

Containers

```
template<typename T>
strong_ordering operator<=>(vector<T> const& lhs, vector<T> const& rhs)
{
    size_t min_size = min(lhs.size(), rhs.size());
    for (size_t i = 0; i != min_size; ++i)
    {
        if (auto const cmp = compare_3way(lhs[i], rhs[i]); cmp != 0)
        {
            return cmp;
        }
    }

    return lhs.size() <=> rhs.size();
}
```

```
template<typename T>
bool operator==(vector<T> const& lhs, vector<T> const& rhs)
{
    // short-circuit on size early
    const size_t size = lhs.size();
    if (size != rhs.size()) {
        return false;
    }

    for (size_t i = 0; i != size; ++i) {
        // use ==, not <=>, in all nested comparisons
        if (lhs[i] != rhs[i]) {
            return false;
        }
    }

    return true;
}
```

Source
P1185R1, Barry Revzin

Containers

- Container types (eg. vector) should implemented operator == to short-circuit comparison (by checking sizes)
- other types containing such types must explicitly implement <=>, ==, and !=
 - because operator == and != invoke <=>

```
struct S
{
    vector<string> names;
    auto operator<=>(S const&) const = default;
    bool operator==(S const& rhs) const { return names == rhs.names; }
    bool operator!=(S const& rhs) const { return names != rhs.names; }
};
```

<=> != == (aka P1185R1)

```
struct A {  
    auto operator<=>(A const&) const = default;  
};
```

<=> != == (aka P1185R1)

```
struct A {  
    auto operator<=>(A const&) const = default;  
};  
struct A {  
    bool operator==(A const&) const = default;  
    auto operator<=>(A const&) const = default;  
};
```

<=> != == (aka P1185R1)

```
struct A {  
    auto operator<=>(A const&) const = default;  
};
```

```
struct A {  
    bool operator==(A const&) const = default;  
    auto operator<=>(A const&) const = default;  
};
```

```
struct B {  
    std::strong_equality operator<=>(B const&) const = default;  
};
```

<=> != == (aka P1185R1)

```
struct A {  
    auto operator<=>(A const&) const = default;  
};
```

```
struct A {  
    bool operator==(A const&) const = default;  
    auto operator<=>(A const&) const = default;  
};
```

```
struct B {  
    std::strong_equality operator<=>(B const&) const = default;  
};
```

```
struct B {  
    bool operator==(B const&) const = default;  
};
```

Two-way comparison generation

For an expression $a@b$, where $@$ is a two-way comparison operator:

- Perform name lookup for $a@b$, $a<=>b$, and $b<=>a$
 - If $@$ is $==$ then $a == b$ and $b == a$
 - If $@$ is $!=$ then $a != b$, $!(a == b)$, $!(b == a)$
- Each potential candidate $<=>$ found is included in overload resolution if:
 - $<=>$ returns `std::*_ordering` and $@$ is one of $==$ $!=$ $<$ $>$ $<=$ $>=$
 - $<=>$ returns `std::*_equality` and $@$ is one of $==$ $!=$
- Select best match with normal overload resolution rules
 - prefer $a@b$ over $a<=>b$ over $b<=>a$ in case of ambiguity
- Finally
 - If $a<=>b$ is the best match, then rewrite $a@b$ to $a<=>b@0$
 - If $b<=>a$ is the best match, then rewrite $b@a$ to $0@b<=>a$

Built-in `<=>` comparisons

Type	Category	Comments
void		Not allowed.
bool	<code>strong_ordering</code>	If only one of the operands is a <code>bool</code> the program is ill-formed.
Integral	<code>strong_ordering</code>	If a narrowing conversion is required, other than from an integral type to a floating point type, the program is ill-formed.
Floating point	<code>partial_ordering</code>	<code>-0 <=> +0</code> yields equivalent <code>NaN <=> anything</code> yields unordered
Object pointer	<code>strong_ordering</code>	Unspecified result if pointers do not point into the same object or array.
Function pointer, pointer to member, <code>nullptr_t</code>	<code>strong_equality</code>	
enumerations	same as underlying type's <code><=></code>	If multiple enumerators have the same value then <code>strong_ordering => weak_ordering</code> <code>strong_equality => weak_equality</code>
(copyable) arrays (<code>T[N]</code>)	same as <code>T</code> 's <code><=></code>	Only when comparing members of a class. Otherwise, ill-formed. Lexicographic elementwise comparison.

Standard library overloads

Non-member operator<=>

`std::pair, std::tuple`

`std::string, std::string_view`

`std::vector, std::array, ...`

`std::shared_ptr, std::unique_ptr`

`std::complex`

`std::optional`

`...`

Further readings

Spaceship Operator

<https://blog.tartanllama.xyz/spaceship-operator/>

Mathematics behind Comparison

<https://foonathan.net/blog/2018/06/20/equivalence-relations.html>

Implementing the spaceship operator for optional

<https://medium.com/@barryrevzin/implementing-the-spaceship-operator-for-optional-4de89fc6d5ec>

Consistent comparison

<http://www.open-std.org/jtc1/sc22/wg21/docs/papers/2017/p0515r2.pdf>

`<=> != ==`

<http://www.open-std.org/jtc1/sc22/wg21/docs/papers/2019/p1185r1.html>

Q&A